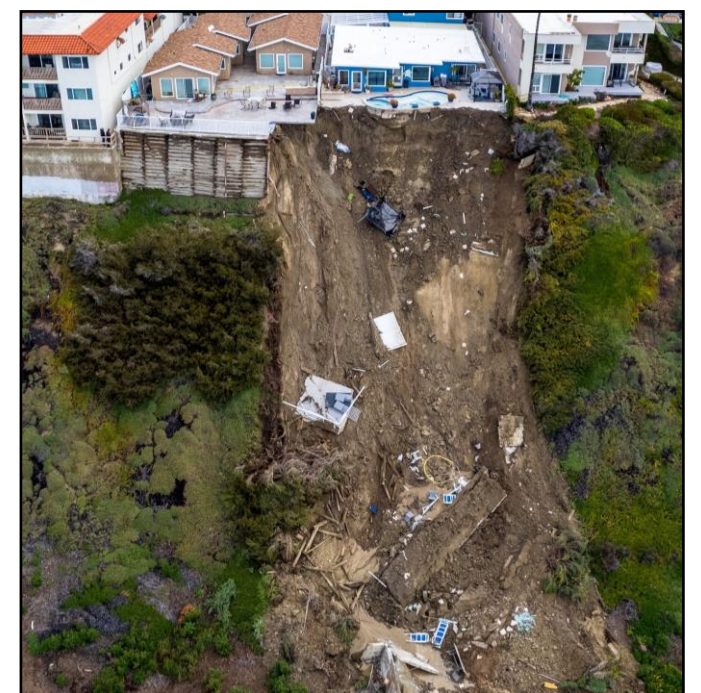


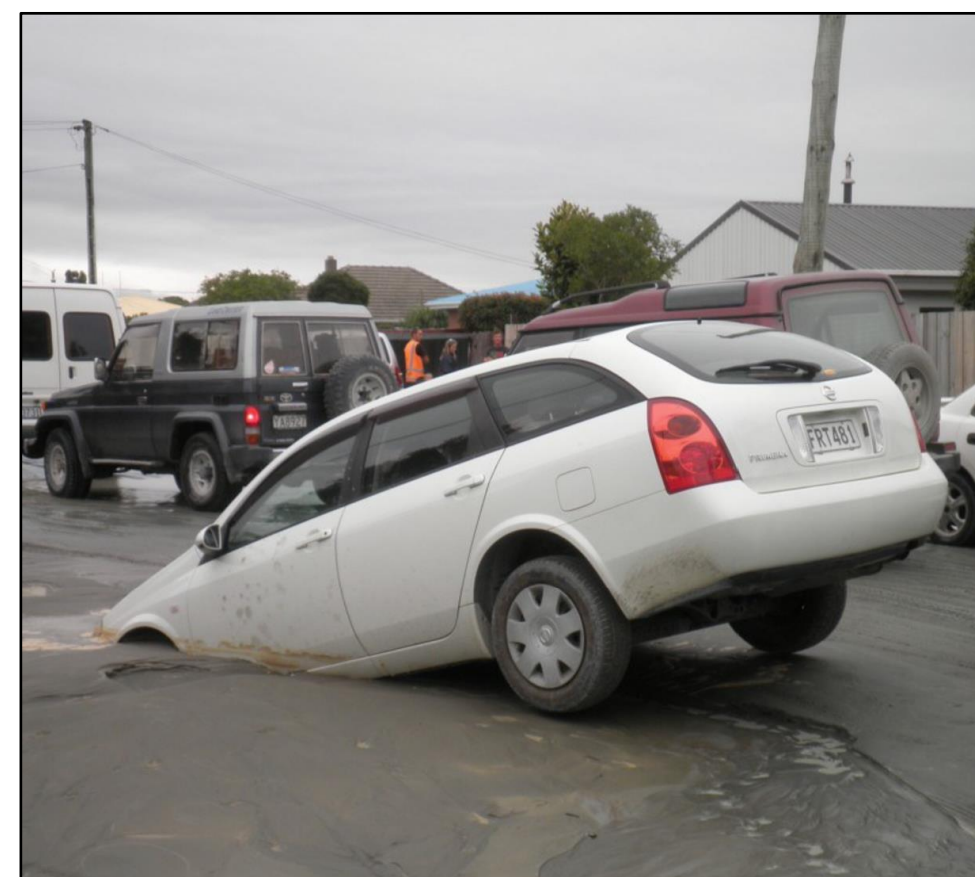
## The Density of Modes (DoM)



We implement a technique (borrowed from thermal systems) to measure the Vibrational Density of Modes (DoM) in granular matter using acoustic excitations.

A March 2023 Landslide in San Clemente, CA [1]

We use the DoM to identify the state of laboratory granular materials, and eventually forecast failure events in earth materials.

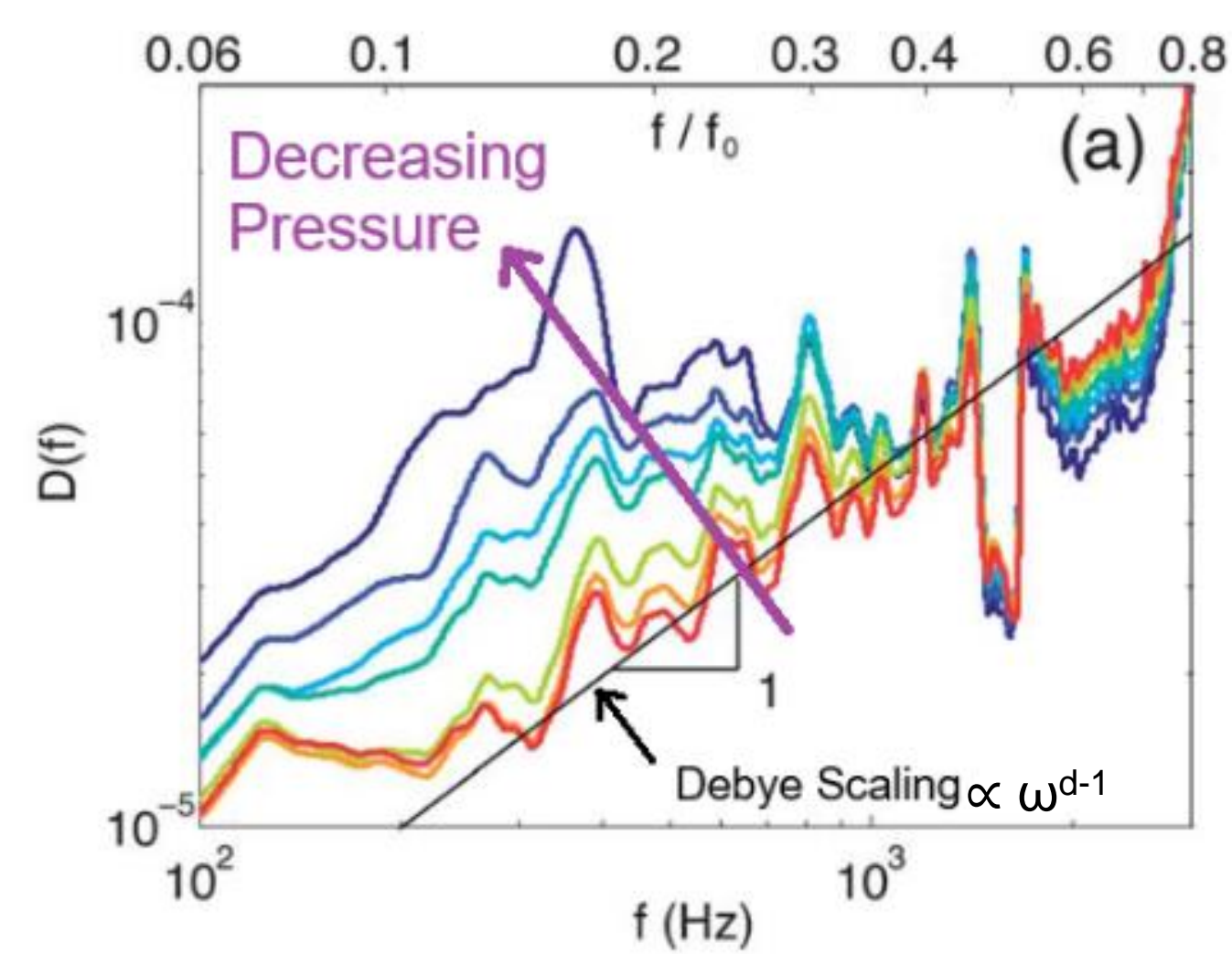


An earthquake causing the ground to liquify [5]

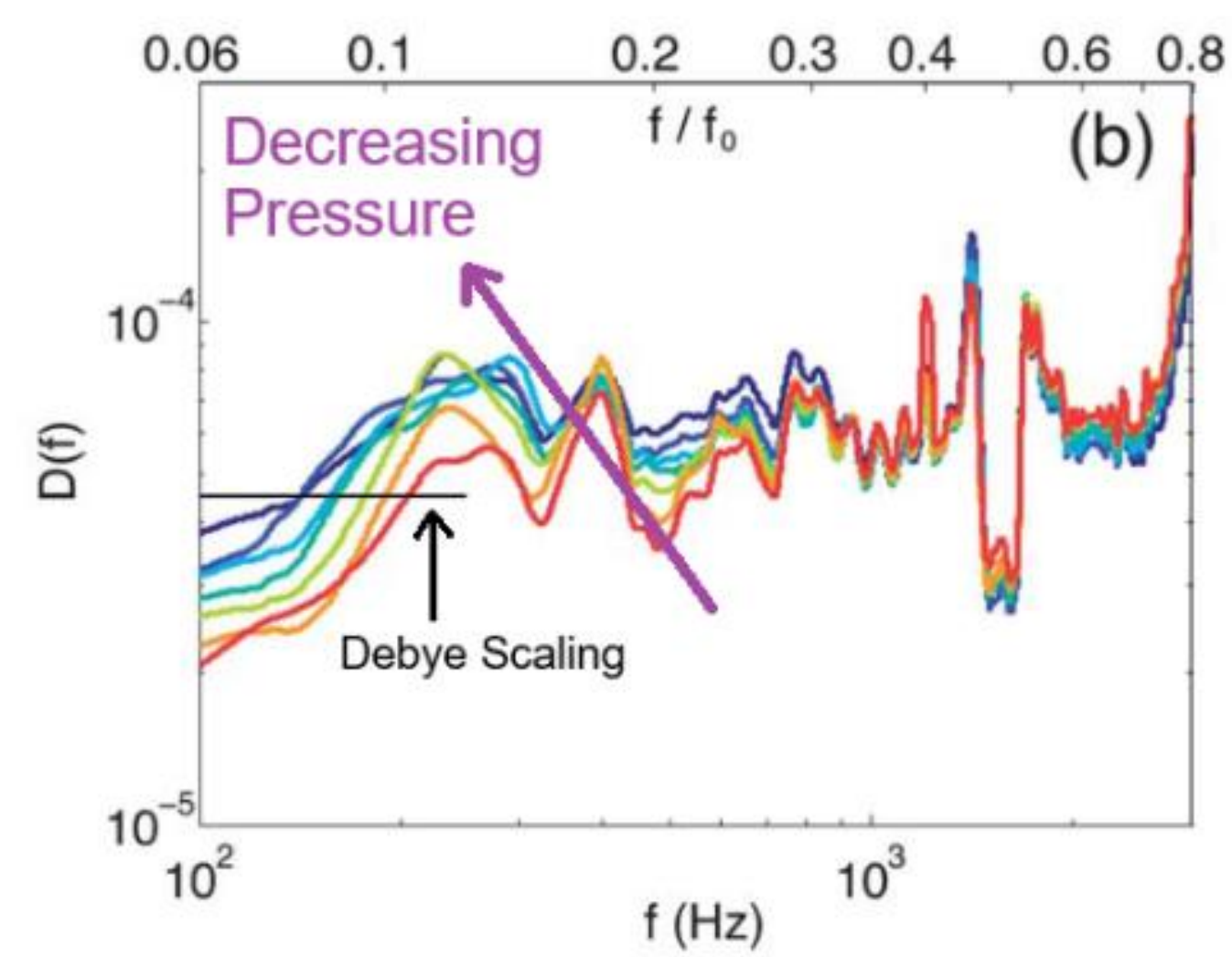
## What is the Density of Modes?

The density of modes  $D(\omega)$  describes the number of modes per unit frequency  $\omega$ . It tells us how many possible ways the system can respond at a given frequency.

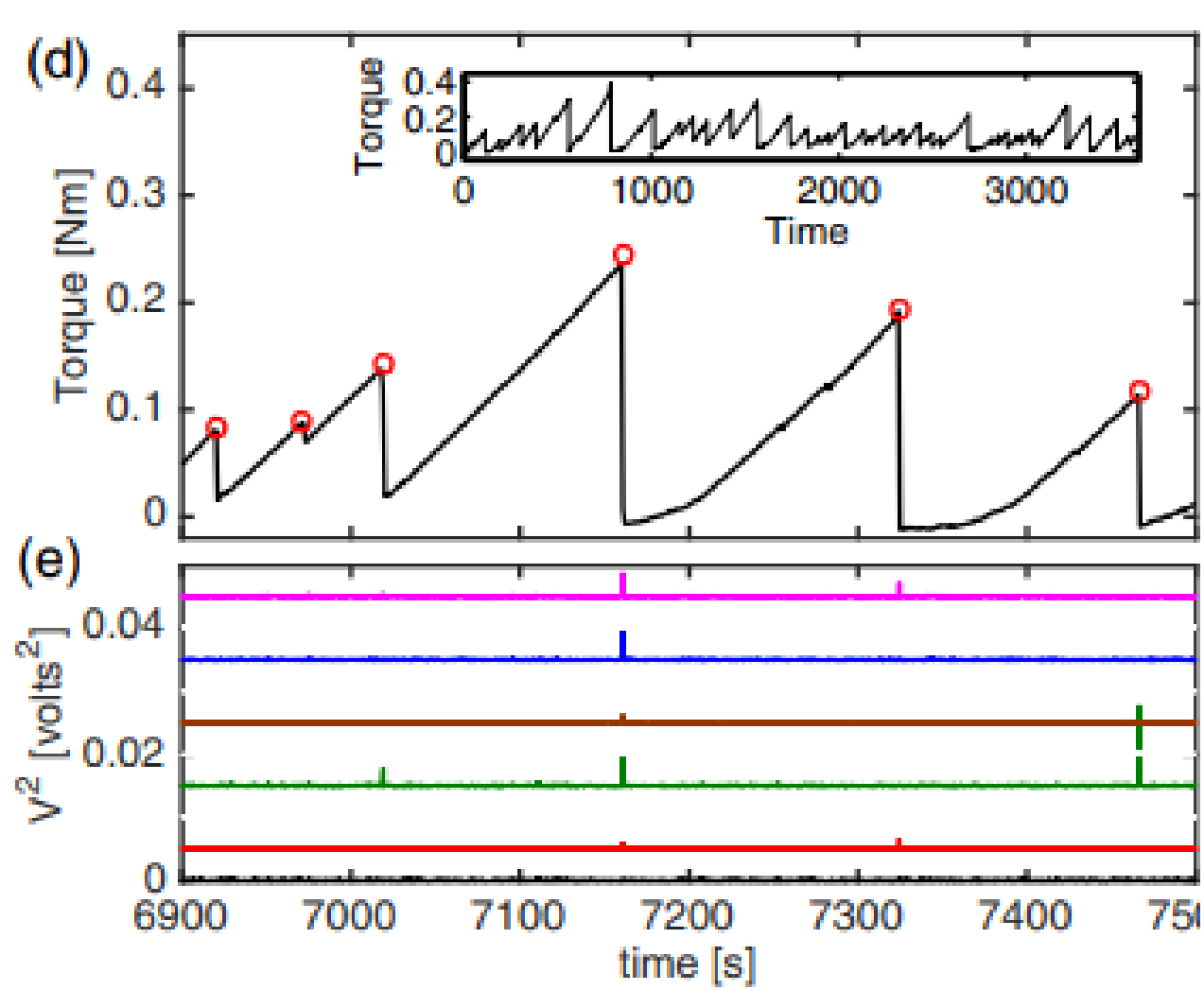
Jammed disordered system: excess low frequency modes relative to Debye-like scaling below some characteristic frequency  $\omega^*$  [6].



ORDERED



DISORDERED



Piezoelectric sensors detect when a granular material fails (marked as red dots) [4].

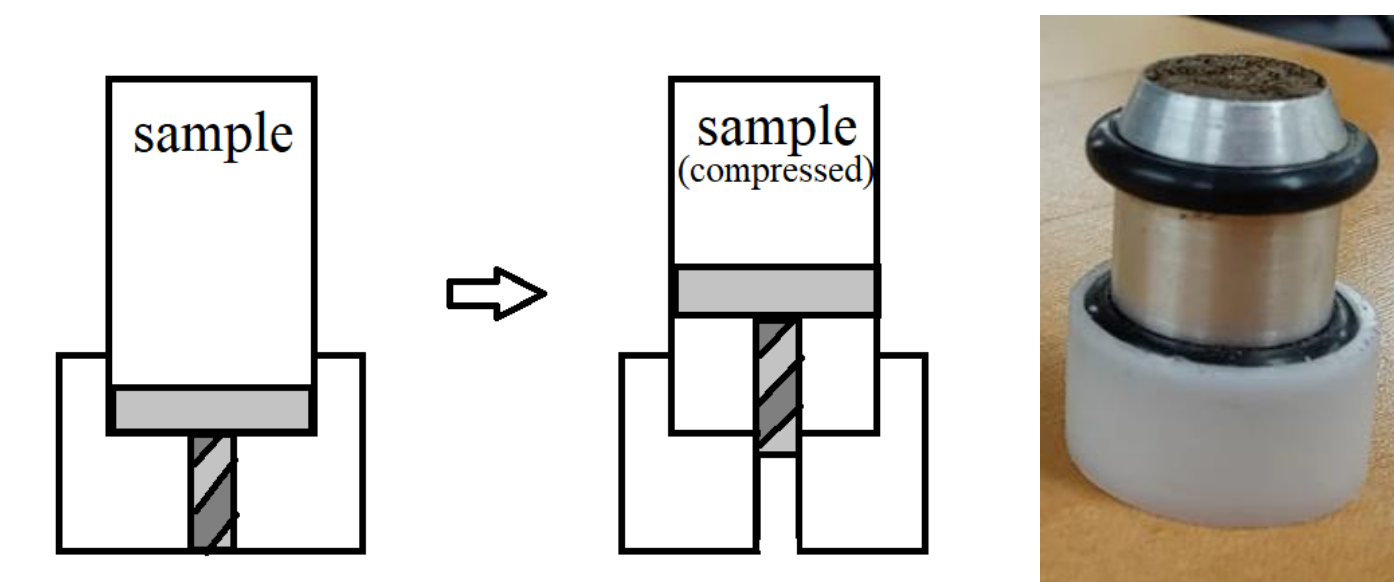
The DoM at 7 pressures for (a) an ordered system (b) a disordered system (Debye scaling is the black line) [2].

## Project Goals: Using the DoM to forecast geohazards:

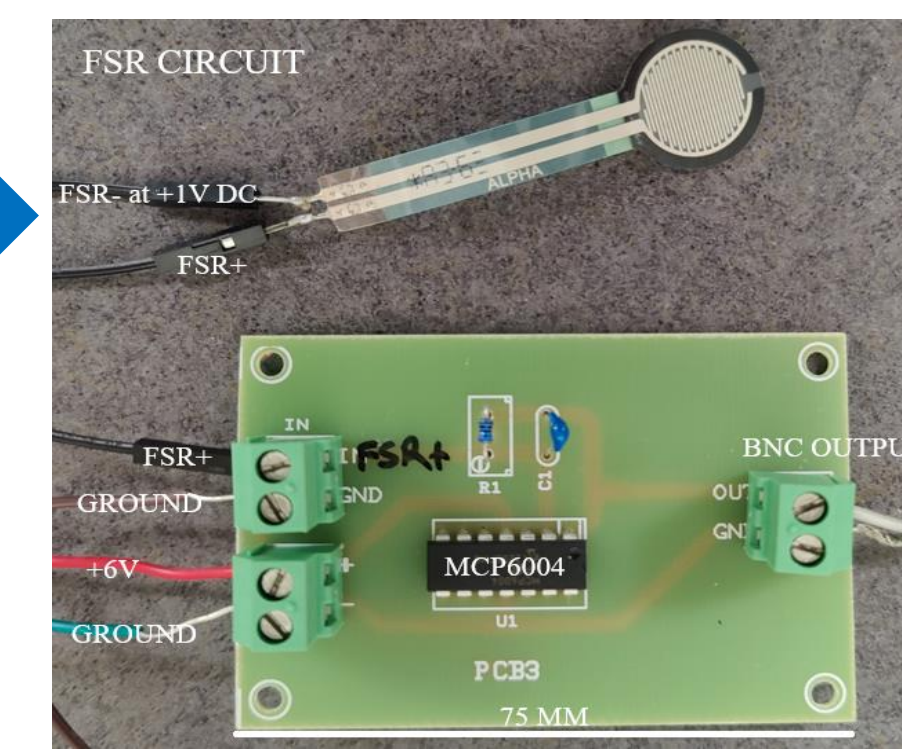
- An excess of low frequency modes in the DoM indicate softer material response.
- Changes in granular structure, applied stress, etc. will change the shape of  $D(\omega)$ .
- The goal: To quantify the changes in the DoM to understand when failure is likely.

## Instrumentation

### 1. Apply constant compressive strain to the sample → with an FSR



A sample being placed under constant compressive strain using a screw.



The force sensitive resistor

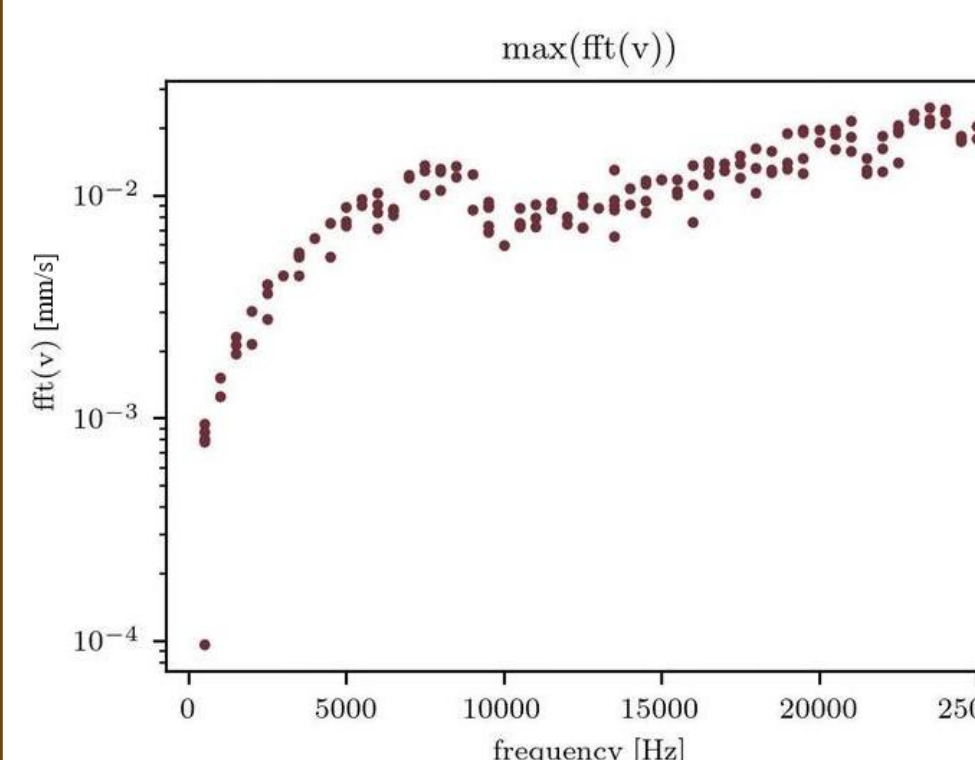
### 2. Acoustic perturbation → using a piezostack



Piezoelectric stacks apply a constant acoustic perturbation to a sample of grains using a high voltage amplifier.

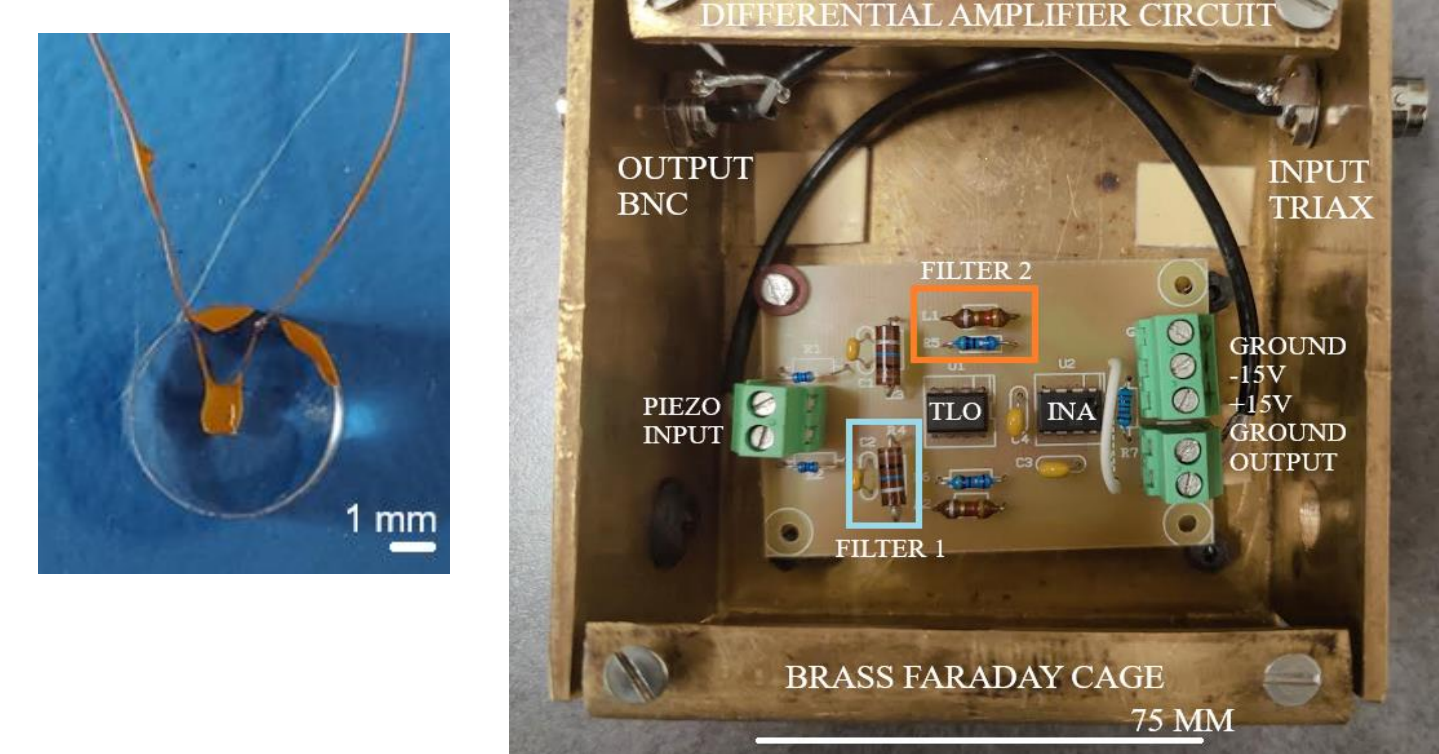
#### Input wave:

- Gaussian White Noise
- SD: 1.2V
- Mean: 3.95V



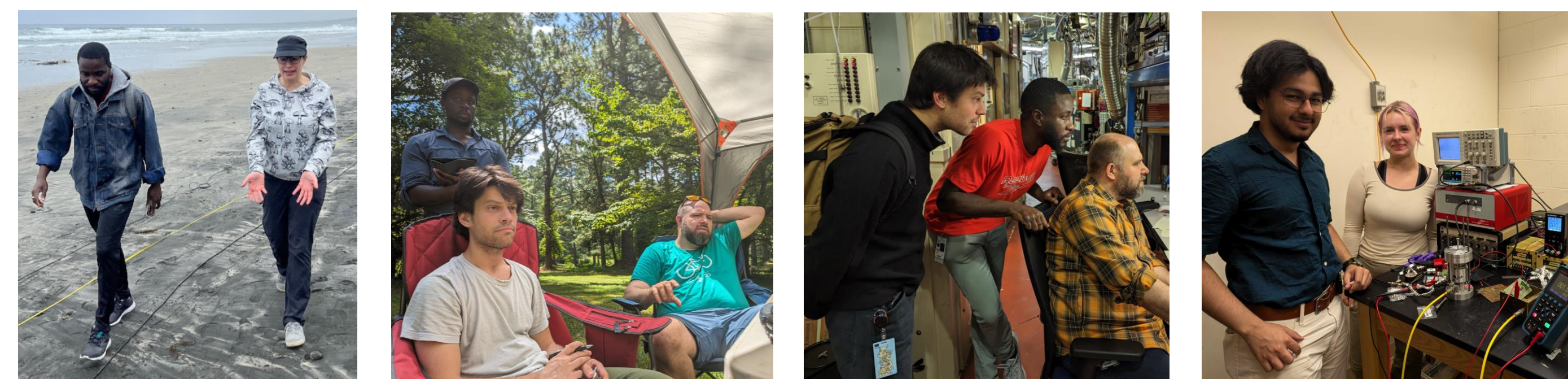
A frequency response curve for the piezostack

### 3. Measuring DoM → using a piezoelectric ceramic



The piezoelectric sensor and amplification circuit

## Meet The DoMinators:



## Comparing Field and Lab DoMs

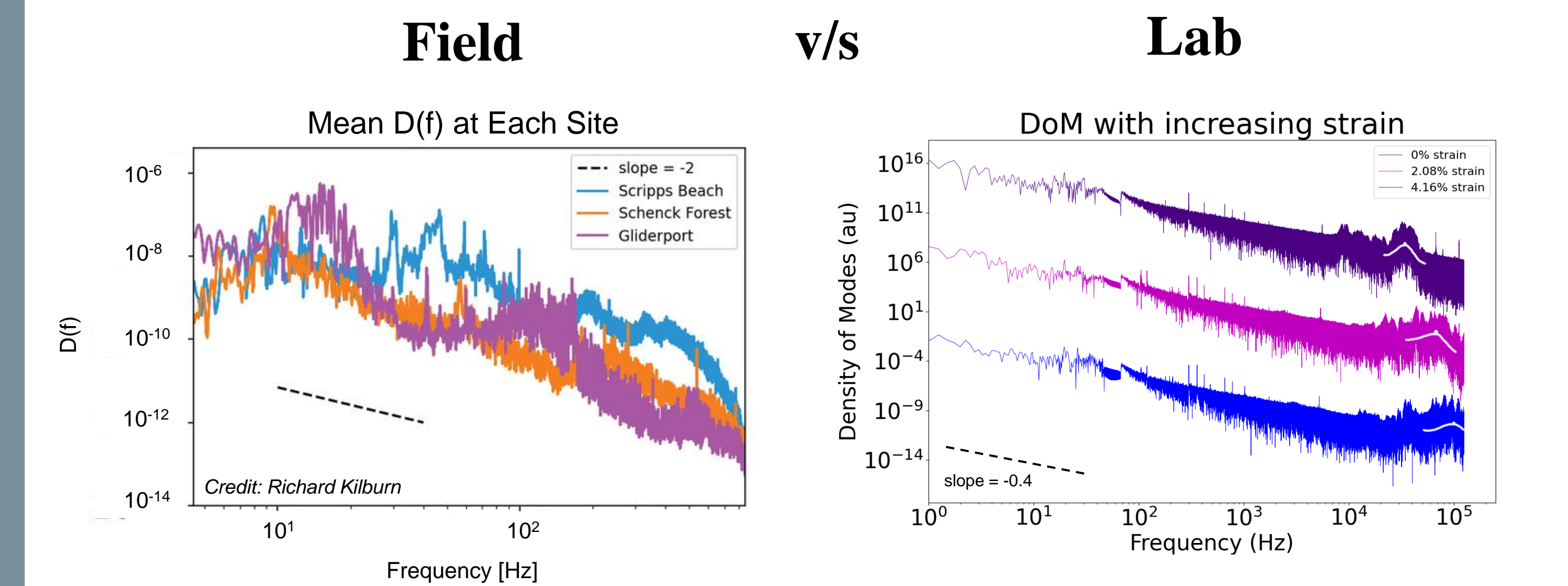
$v(t)$  is obtained by integrating piezoelectric voltage ( $\propto$  particle accelerations) over time.

$$C_v(t) \equiv \frac{\sum_i \langle v_i(\tau+t) \cdot v_i(\tau) \rangle_\tau}{\sum_i \langle v_i(\tau) \cdot v_i(\tau) \rangle_\tau}$$

The Velocity Autocorrelation [3,4]

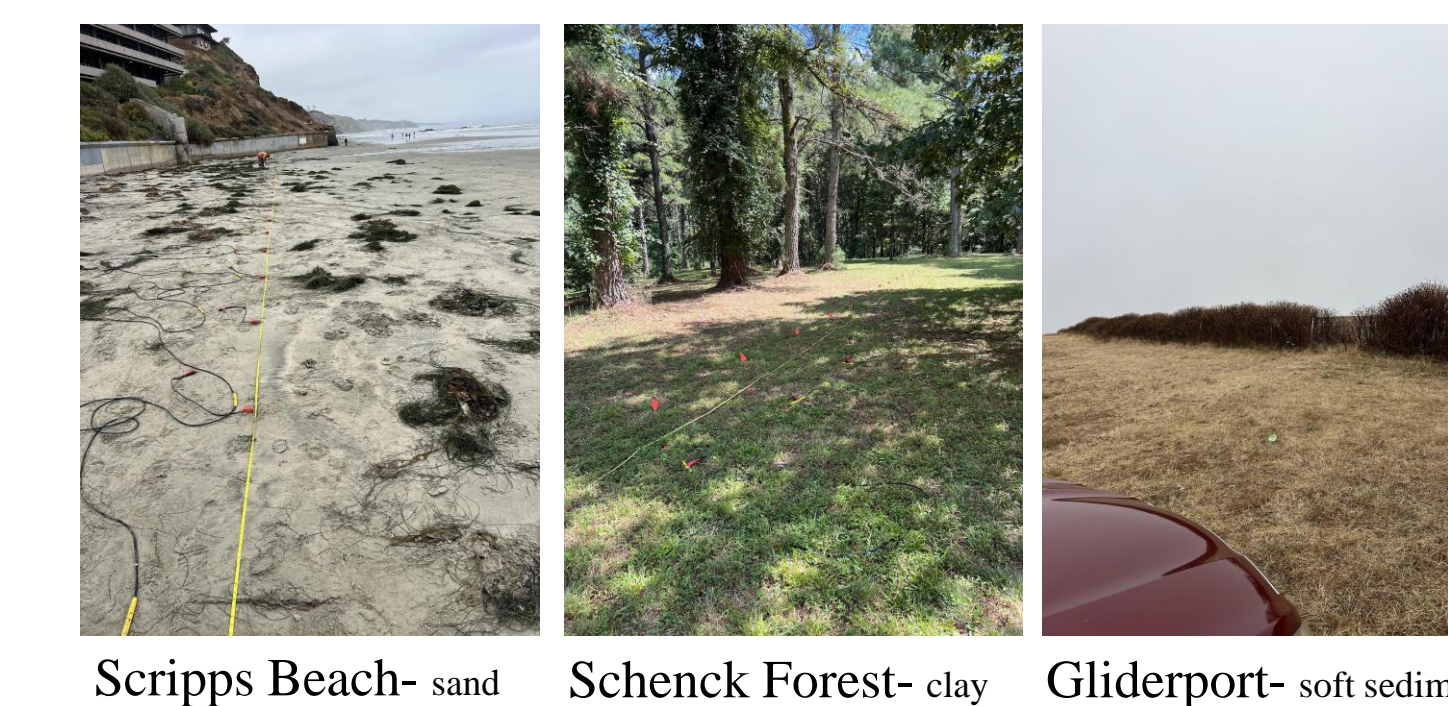
$$D(f) \equiv \int_0^\infty C_v(t) \cos(2\pi ft) dt$$

The DoM [3,4]

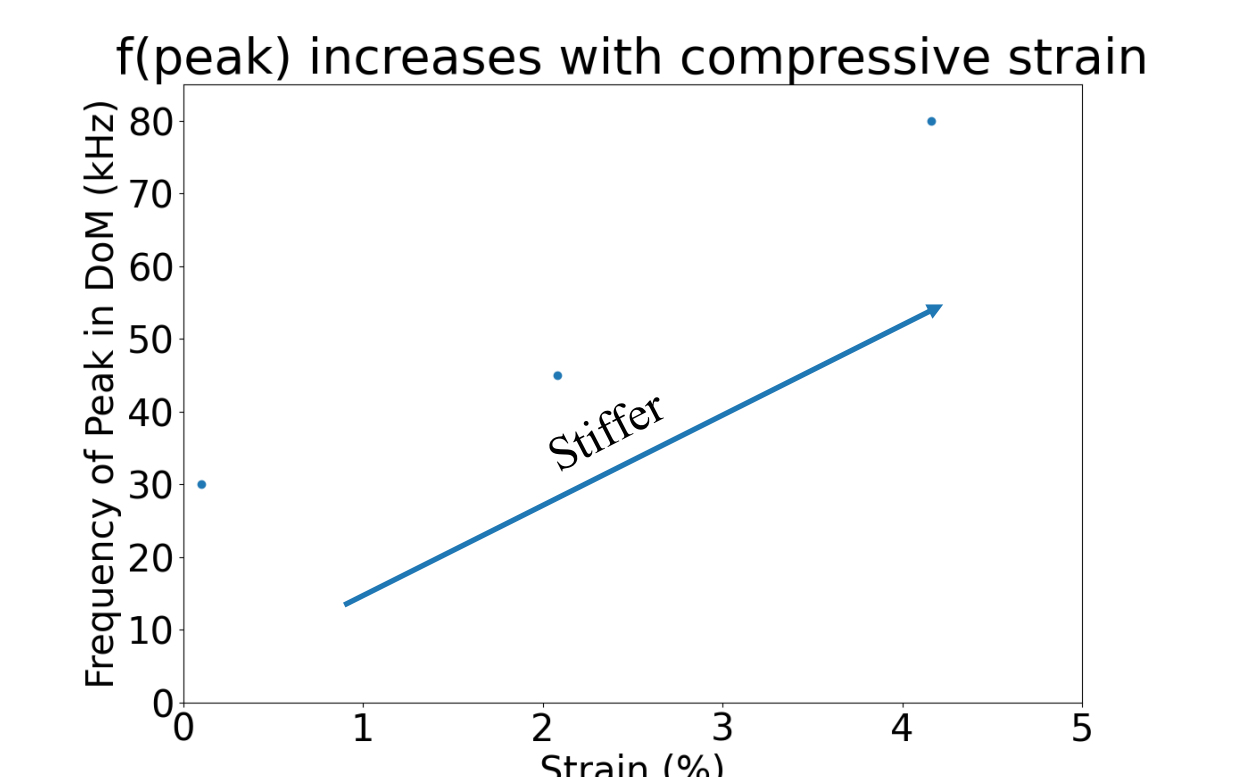


DoM readings from 3 field sites

Effects of low pressure (as a function of strain) on pluviated glass beads (1mm)



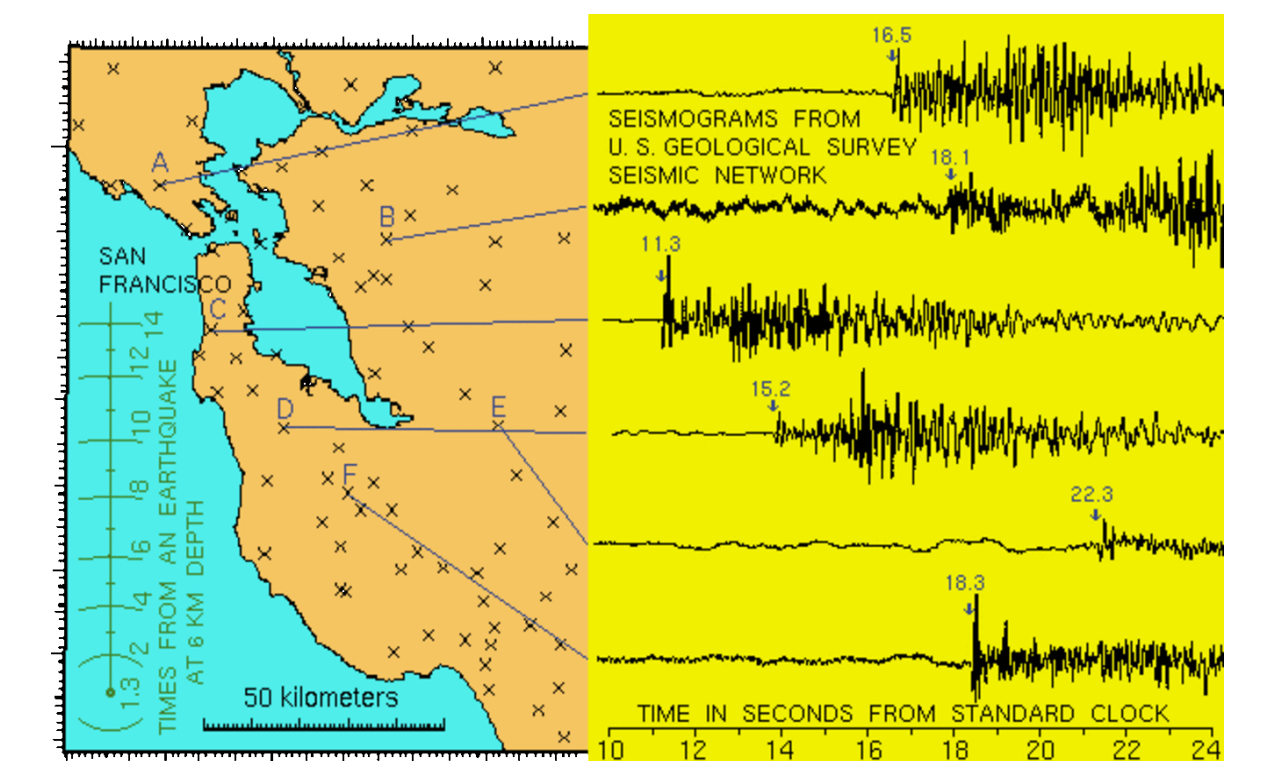
Scripps Beach- sand Schenck Forest- clay Gliderport- soft sediment



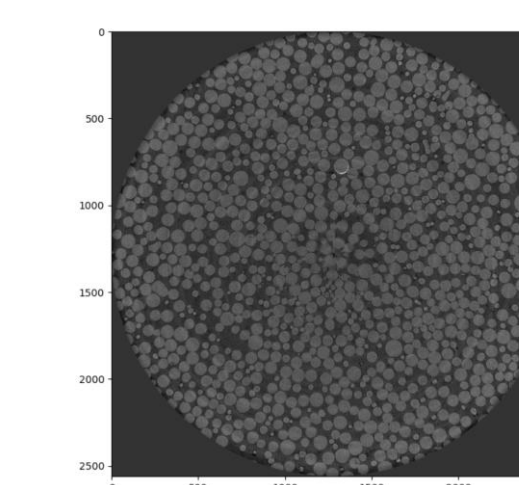
## Outlook

### Calibrating Geological Monitoring Instrumentation:

Soil structure and packing geometry affects the position of low frequency peaks in the DoM. This could calibrate seismographs to forecast when landscapes might fail.



Calibrating geological instrumentation [7]



An  $\mu$ -CT of some glass beads.

### Using tomography to understand 3D structure:

We can take a micro-tomography scan before and after DoM measurements and reconstruct 3D structure to see how changes in packings are reflected in the DoM.

## References

[1] J Smith, Article: San Clemente Times, 032223. [5] Lincoln, Mark. Christchurch Earthquake, 23-07-24  
[2] Owens and Daniels, Soft Matter 9, 1214-1219. [6] N. Xu, M. Wyart, A. J. Liu, and S. R. Nagel, Physical Review Letters 98, 175502  
[3] Dickey, J. M., and Arthur Paskin. Physical Review 188, 1407. [7] US Geological Survey, Maps of Seismic Stations.  
[4] Theodore A. Brzinski, III, and Karen E. Daniels. Physical Review Letters 188, 1407. [8] S. A. Blue, S. C. Wright, and E. T. Owens, arXiv:2403.10322.